

# ROMANIAN MATHEMATICAL MAGAZINE

In  $\triangle ABC$  the following relationship holds:

$$\frac{a^3}{(b+c)^3 - a^3} + \frac{b^3}{(c+a)^3 - b^3} + \frac{c^3}{(a+b)^3 - c^3} \geq \frac{3}{7}$$

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Solution by Tapas Das-India

$$\begin{aligned} LHS &= \sum \frac{(b+c)^3}{(b+c)^3 - a^3} - 3 = \sum \frac{1}{1 - \left(\frac{a}{b+c}\right)^3} - 3 \stackrel{\text{Bergstrom}}{\geq} \\ &\geq \frac{9}{3 - \sum \left(\frac{a}{b+c}\right)^3} - 3 \stackrel{\text{CBS}}{\geq} \frac{9}{3 - \frac{1}{9} \sum \left(\frac{a}{b+c}\right)^3} - 3 \stackrel{\text{Nesbitt}}{\geq} \\ &\geq \frac{9}{3 - \frac{1}{9} \cdot \frac{27}{8}} - 3 = \frac{24}{7} - 3 = \frac{3}{7} \end{aligned}$$

Equality for  $a = b = c$