

ROMANIAN MATHEMATICAL MAGAZINE

If $a, b, c, d \in R$, $a + b + c + d = 4$ then:

$$(a^4 + 3)(b^4 + 3)(c^4 + 3)(d^4 + 3) \geq 256$$

Proposed by Nguyen Hung Cuong-Vietnam

Solution by Tapas Das-India

$$(a^4 + 3)(b^4 + 3)(c^4 + 3)(d^4 + 3) =$$

$$(a^4 + 1 + 1 + 1)(1 + b^4 + 1 + 1)(1 + 1 + c^4 + 1)(1 + 1 + 1 + d^4) \stackrel{\text{Holder}}{\geq}$$

$$\geq (a + b + c + d)^4 = 4^4 = 256$$

Equality for $a = b = c = d = 1$