

ROMANIAN MATHEMATICAL MAGAZINE

S.2450 If $x, y, z > 0$, then:

$$\frac{x}{(x+1)(z+1)} + \frac{y}{(y+1)(x+1)} + \frac{z}{(z+1)(y+1)} + \frac{xyz+1}{(x+1)(y+1)(z+1)} = 1.$$

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Clearing denominators, the desired identity is equivalent to

$$\begin{aligned}x(y+1) + y(z+1) + z(x+1) + xyz + 1 &= (x+1)(y+1)(z+1) \\xy + x + yz + y + zx + z + xyz + 1 &= xyz + xy + xz + x + yz + y + z + 1,\end{aligned}$$

which is true.